國立臺北科技大學

九十九學年第二學期電機系博士班資格考試

通訊系統(大學部) 試題

第一頁 共三頁



<u>注意事項</u>:

本試題共【4】題,配分共100分。
請按順序標明題號作答,不必抄題。
全部答案均須答在試卷答案欄內,否則不予計分。
考試時間:二小時。

1. Given a filter with frequency response function

$$H(f) = \frac{5}{4 + j(2\pi f)}$$

and input $x(t) = e^{-3t}u(t)$, obtain and plot the energy spectral density for

(10%) (a) the input signal x(t)

(15%) (b) the output signal, if x(t) is the input to the filter

2. In a digital communication system, a root-raised cosine (RRC) filter is frequently used as the transmit and receiver filter. A RRC filter $H_{RRC}(f)$ is defined as

$$H_{RC}(f) = H_{RRC}(f)H_{RRC}(f),$$

where

$$H_{RC}(f) = \begin{cases} T, & 0 \le |f| \le \frac{1-\alpha}{2T} \\ \frac{T}{2} \left[1 + \cos \frac{\pi T}{\alpha} \left(|f| - \frac{1-\alpha}{2T} \right) \right], & \frac{1-\alpha}{2T} \le |f| \le \frac{1+\alpha}{2T} \\ 0, & |f| > \frac{1+\alpha}{2T} \end{cases}$$

is the raised cosine (RC) filter. Explain in details what rules the RRC filters play from the following aspects:

- (10%) (a) Output SNR of the receiver
- (15%) (b) Bandlimited channel

3. Consider the system shown below. Assume the average value of m(t) is zero and the maximum value of |m(t)| is M. Suppose m(t) is a narrowband signal within maximal frequency W. Assume the square-law device is defined by $y(t) = 4x(t) + 2x^2(t)$



- (10%) (a) Derive the signal y(t).
- (15%) (b) Design the filter that yields an AM signal for g(t).

4. Consider the QPSK demodulator shown below. Assume the QPSK modulator produces a phase imbalanced signal of the form

$$x_{c}(t) = Ad_{1}(t)\cos(2\pi f_{c}t + \beta/2) - Ad_{2}(t)\sin(2\pi f_{c}t - \beta/2)$$

where $d_1(t)$ and $d_2(t)$ are "+1" or "-1" of duration T with equal probability and $\beta \neq 0$. Assume the system is synchronized in terms of time slots. Assume n(t) is additive white Gaussian noise with double-sided power spectral density $N_0/2$.



- (10%) (a) Find the integrator outputs, i.e., $V_1(t)$ and $V_2(t)$.
- (15%) (b) Find the probability of error per quadrature channel.