## 國立臺北科技大學

# 103 學年第一學期電機系博士班資格考試

### 數位通訊理論 試題

### 第一頁 共二頁



- 注意事項:
  1. 本試題共【5】題,配分共100分。
  2. 請按順序標明題號作答,不必抄題。
  3. 全部答案均須答在試卷答案欄內,否則不予計分。
  4. 考試時間:二小時。

#### 1. (20%)

The random process X(t) is defined by  $X(t) = X \cos(2\pi f_0 t) + Y \sin(2\pi f_0 t)$ , where X and Y are two zero-mean independent Gaussian random variables each with the variance  $\sigma^2$ . Please find the autocorrelation function and power spectral density of X(t).

#### 2. (20%)

For a BFSK system, the two signals are defined by  $s_1(t) = \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_1 t)$  and

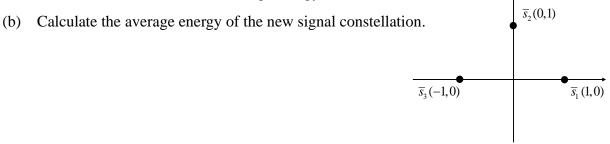
$$s_2(t) = \sqrt{\frac{2E_b}{T_b}} \cos(2\pi f_2 t), \quad 0 \le t \le T_b.$$
 In the presence of additive white Gaussian noise of

zero mean and power spectral density  $\frac{N_0}{2}$ , calculate the average probability of error.

#### 3. (20%)

Consider the signal constellation as shown in Figure P-3. The *a priori* probabilities for  $\overline{s_1}$ ,  $\overline{s_2}$ , and  $\overline{s_3}$  are 0.5, 0.3, and 0.2, respectively.

(a) Find the translation vector to translate the signal constellation into a new signal constellation with minimum average energy.





#### 4.(20%)

A source emits one of three symbols  $s_1$ ,  $s_2$ , and  $s_3$  with probabilities 0.5, 0.25, and 0.25, respectively. The successive symbols emitted by the source are statistically independent. Calculate the entropy of the source.

#### 5. (20%)

The trellis diagram of a (2,1,2) convolutional code is shown in Figure P-5. If the received sequence is 11 00 01 00. Using the Viterbi algorithm, compute the decoded sequence.

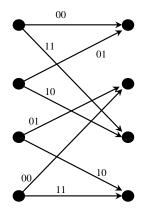


Figure P-5