

國立臺北科技大學  
九十七學年第一學期電機系博士班資格考試

模糊控制試題

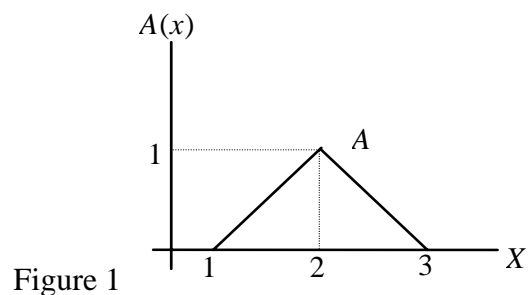
第一頁 共二頁

**注意事項：**

1. 本試題共【5】題，配分共 100 分。
2. 請按順序標明題號作答，不必抄題。
3. 全部答案均須答在試卷答案欄內，否則不予計分。
4. 考試時間：二小時。

- (1) (a) Please give an illustration for fuzzy set and define its fuzzy membership function? Explain them in detail too. ( If you just plot without any explanation for the fuzzy set meaning, there will be no points) (10%)
- (b) Plot fuzzy sets intersection and explain what the practical meaning of it is. (If you just plot it without any explanation, there will be no points) (10%)
- (c) Please use an example to explain what is the fuzzy relation? (10%)

- (2) By Extension Principle, please plot  $f(A)(y)$ , where  $f(x) = y = \begin{cases} 2, & x \leq 2 \\ 3x, & \text{others} \end{cases}$  and the fuzzy set A is shown in Figure 1. (10%)



- (3) In GMP (Generalized Modus Ponens), there is  $B'(y) = \max\{\min[A'(x), (A \rightarrow B)(x, y)]\}$ . By using Dienes-Rescher Implication:  $Fp1 \rightarrow Fp2 \Leftrightarrow \max[1 - Fp1(x), Fp2(y)]$ , now, we have  $A = 0.6/x_1 + 1/x_2 + 0.7/x_3$ ,  $B = 0.4/y_1 + 0.9/y_2$ , and  $A' = 0.5/x_1 + 0.9/x_2 + 0.5/x_3$ . What is

the conclusion “y is B’ ”? That is B’=? (20%)

(4) Please find  $W = P^{-1} \circ Q^{-1}$ , where  $\circ$  is the Max-min operation. (10%).

$$P = \begin{bmatrix} 1 & 0.7 & 0.5 \\ 0.7 & 1 & 0.5 \\ 0.5 & 0.5 & 1 \end{bmatrix}, \quad Q = \begin{bmatrix} 0.2 & 0.7 & 0.4 \\ 0.1 & 0.5 & 0 \\ 0 & 0.6 & 0.1 \end{bmatrix}$$

(5) We have to control an inverted pole, the fuzzy variables  $(\theta, \dot{\theta}, u)$  and the control rule table are shown in the following Figure 2 and Table 1, respectively. Please use Minimum Inference Engine and Center of Gravity Defuzzification to find the control output U, while the singleton input is  $(\theta = 12, \dot{\theta} = -15)$ . (30%)

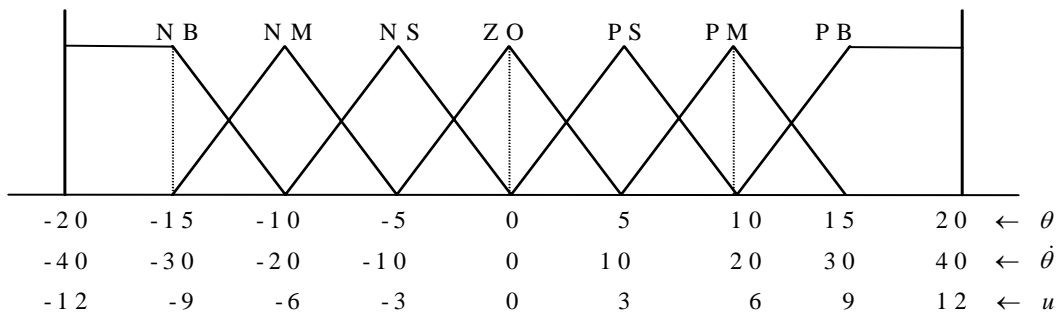


Figure 2

| $\theta \backslash \dot{\theta}$ | N B | N M | N S | Z O | P S | P M | P B |
|----------------------------------|-----|-----|-----|-----|-----|-----|-----|
| N B                              | N B | N B | N B | N B | N M | N M | N S |
| N M                              | N B | N B | N M | N M | N S | Z O | Z O |
| N S                              | N B | N M | N S | N S | Z O | P S | P M |
| Z O                              | N B | N M | N S | Z O | P S | P M | P B |
| P S                              | N M | N S | Z O | P S | P S | P M | P B |
| P M                              | Z O | Z O | P S | P M | P M | P B | P B |
| P B                              | P S | P M | P M | P B | P B | P B | P B |

Table 1